

Math 16C

Kouba

You Must Know These

$$1.) \quad 1 + 2 + 3 + 4 + \cdots + n = \frac{n(n+1)}{2}$$

$$2.) \quad 1 + r + r^2 + r^3 + r^4 + \cdots + r^n = \frac{1 - r^{n+1}}{1 - r} \quad \text{for any } r \neq 1.$$

$$3.) \quad 1 + r + r^2 + r^3 + r^4 + r^5 + \cdots = \frac{1}{1 - r} \quad \text{for } -1 < r < 1.$$

$$4.) \quad \frac{1}{(n+1)^p} + \frac{1}{(n+2)^p} + \frac{1}{(n+3)^p} + \frac{1}{(n+4)^p} + \cdots < \frac{n^{1-p}}{p-1}$$

for any convergent p-series ($p > 1$).