**RECALL**: Consider two points  $(x_1, y_1)$  and  $(x_2, y_2)$  in two-dimensional space. The midpoint of the line segment joining these two points is given by

space. The midpoint of the line segment joining these two points is given by
$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right) \cdot (x_1, y_1)$$
The distance between 
$$(x_1, y_1)$$
 these two points is

$$D = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

RECALL: The set of all points (x, y) in two-dimensional space which are a distance r from a fixed point (h, k) is a circle (with center (h, k) and radius r) given by the equation

$$(x-h)^2 + (y-k)^2 = r^2$$
. (h, k)

Let  $(x_1, y_1, z_1)$  and  $(x_2, y_2, z_2)$  be two points in three-dimensional space. The midpoint of the line segment joining these two points is given by

The distance between the time segment joining these two points is given by
$$\begin{pmatrix}
x_{1} + x_{2} & y_{1} + y_{2} \\
2 & 2
\end{pmatrix}, \quad \begin{pmatrix}
x_{1}, y_{1}, z_{1}
\end{pmatrix}$$
The distance between these two points is
$$(x_{1}, y_{1}, z_{1}) \\
(x_{2}, y_{2}, z_{2})$$
These two points is

**DEFINITION**: The set of all points (x, y, z) in three-dimensional space which are a distance r from a fixed point (h, k, l) is a sphere (with center (h, k, l) and radius r given by the equation

$$(x-h)^2 + (y-k)^2 + (z-1)^2 = r^2$$
.

Example: Find the center and radius of each of the following spheres.

1. 
$$2 x^2 + 2 y^2 + 2 z^2 = 32$$
  
center (0, 0, 0) radius 4  
2.  $x^2 + y^2 + z^2 - 4 x + 6 y = 17$   
center (2,-3, 0) radius  $\sqrt{30}$ 

Example: The diameter of a sphere has endpoints (1, 3, 0) and (-2, 4, 6). Determine an equation for this sphere.

$$(x + 1/2)^2 + (y-7/2)^2 + (z-3)^2 = 23/2$$

Example: Find and simplify an equation for all points (x, y, z) in three-dimensional space which are equidistant from the point (1,-2,3) and the plane z=-1.

$$z = 1/8 (x-1)^2 + 1/8 (y+2)^2 + 1$$