

Math 21B (Winter 2006)
Kouba
Exam 2

Please PRINT your name here :

Your Exam ID Number

1. PLEASE DO NOT TURN THIS PAGE UNTIL TOLD TO DO SO.
2. IT IS A VIOLATION OF THE UNIVERSITY HONOR CODE TO, IN ANY WAY, ASSIST ANOTHER PERSON IN THE COMPLETION OF THIS EXAM. IT IS A VIOLATION OF THE UNIVERSITY HONOR CODE TO COPY ANSWERS FROM SOMEONE ELSE'S EXAM. PLEASE KEEP YOUR OWN WORK COVERED UP AS MUCH AS POSSIBLE DURING THE EXAM SO THAT OTHERS WILL NOT BE TEMPTED OR DISTRACTED. THANK YOU FOR YOUR COOPERATION.
3. No notes, books, or classmates may be used as resources for this exam. YOU MAY USE A CALCULATOR ON THIS EXAM.
4. Read directions to each problem carefully. Show all work for full credit. In most cases, a correct answer with no supporting work will NOT receive full credit. What you write down and how you write it are the most important means of your getting a good score on this exam. Neatness and organization are also important.
5. Make sure that you have 6 pages, including the cover page.
6. You will be graded on proper use of integral and derivative notation.
7. Include units on answers where units are appropriate.
8. You have until 11:50 a.m. to finish the exam.

1.) (12 pts.) The base of a solid lies in the region bounded by the graphs of $y = x^2$, $y = 0$, and $x = 2$. Cross-sections of the solid taken perpendicular to the x -axis at x are rectangles of height 5. SET UP BUT DO NOT EVALUATE an integral which represents the volume of this solid.

2.) (12 pts.) A flat plate of *variable* density lies in the region bounded by the graphs of $y = 3 + \sin x$, $y = 0$, $x = 0$, and $x = 2\pi$. Density at point (x, y) is given by $\delta(x, y) = 3 + \sqrt{x}$. SET UP BUT DO NOT EVALUATE integrals which represent \bar{y} , the y -coordinate for the *center of mass* of this plate.

3.) (6 pts. each) Consider the region bounded by the graphs of $y = \ln x$, $y = 0$, and $x = e$. SET UP BUT DO NOT EVALUATE integrals which represent the volume of the solid formed by revolving this region about

a.) the x -axis using the DISC METHOD.

b.) the y -axis using the SHELL METHOD.

c.) the line $x = -1$ using the DISC METHOD.

d.) the line $y = 2$ using the SHELL METHOD.

4.) (13 pts.) Set up and EVALUATE an integral which represents the *arc length* of the following curve, which is given by $y = \frac{1}{2}(3x)^{2/3}$ for $0 \leq x \leq 1$.

5.) (13 pts.) A chain weighs 2 pounds per foot and is used to raise a 100 pound object on the ground to a point 50 feet above the ground. Set up and EVALUATE an integral which represents the work required to complete the task (Include the weight of the chain in your solution.)

6.) (13 pts.) A flat plate is in the shape of a right triangle with legs 3 feet and 4 feet. It rests vertically on its 4-foot edge at the bottom of a pool filled to a depth of 8 feet. SET UP BUT DO NOT EVALUATE an integral which represents the force (on one side) of water pressure on this plate. (Water weighs 62.4 pounds per cubic foot.)

7.) (13 pts.) The semi-circle $y = \sqrt{1 - x^2}$ for $-1 \leq x \leq 1$ is rotated about the x -axis to form a sphere. Set up and EVALUATE an integral which represents the *surface area* of this sphere.

The following EXTRA CREDIT problem is OPTIONAL. It is worth 10 points.

1.) A circle has radius a units. Its center is b units from line L . The circle is rotated about line L to form a torus (doughnut). Use integration to compute the volume of the torus.