

1.) Compute the divergence of \vec{F} and the curl of \vec{F} for each of the following vector fields.

a.) $\vec{F}(x, y, z) = (x^4)\vec{i} + (-x^3 z^2)\vec{j} + (4xy^2 z)\vec{k}$

b.) $\vec{F}(x, y, z) = (xy \sin z)\vec{i} + (\cos(xz))\vec{j} + (y \cos z)\vec{k}$

2.) Verify Stoke's Theorem for $\vec{F}(x, y, z) = (y^2)\vec{i} + (x)\vec{j} + (z^2)\vec{k}$, where surface S is that portion of the paraboloid $z = x^2 + y^2$ below the plane $z = 1$.

3.) Use Stoke's Theorem to evaluate $\int \int_S \nabla \times \vec{F} \cdot \vec{n} \, dS$, where

$\vec{F}(x, y, z) = (yz)\vec{i} + (xz)\vec{j} + (xy)\vec{k}$ and surface S is that portion of the paraboloid $z = 9 - x^2 - y^2$ above the plane $z = 5$.

4.) Use Stoke's Theorem to evaluate $\oint_C \vec{F} \cdot \vec{T} \, ds$, where $\vec{F}(x, y, z) = (e^{-x})\vec{i} + (e^x)\vec{j} + (e^z)\vec{k}$ and surface S is that portion of the plane $2x + y + 2z = 2$ in the first octant.

5.) Verify the Divergence Theorem for $\vec{F}(x, y, z) = (xy)\vec{i} + (yz)\vec{j} + (xz)\vec{k}$, where the solid D is the cylinder $x^2 + y^2 = 1$ for $0 \leq z \leq 1$.

6.) Use the Divergence Theorem to evaluate $\int \int_S \vec{F} \cdot \vec{n} \, dS$, where

$\vec{F}(x, y, z) = (e^x \sin y)\vec{i} + (e^x \cos y)\vec{j} + (yz^2)\vec{k}$ and surface S is the box bounded by the planes $x = 0, x = 1, y = 0, y = 1, z = 0,$ and $z = 2$.

7.) Use the Divergence Theorem to evaluate $\int \int \int_D \text{div } \vec{F} \, dV$, where

$\vec{F}(x, y, z) = (xe^y)\vec{i} + (xz)\vec{j} + (x \sin z)\vec{k}$ and the solid D is the cube with vertices $(0, 0, 0), (1, 0, 0), (0, 1, 0),$ and $(0, 0, 1)$.

"An individual has not started living until he can rise above the narrow confines of his individualistic concerns to the broader concerns of all humanity." - Martin Luther King, Jr.