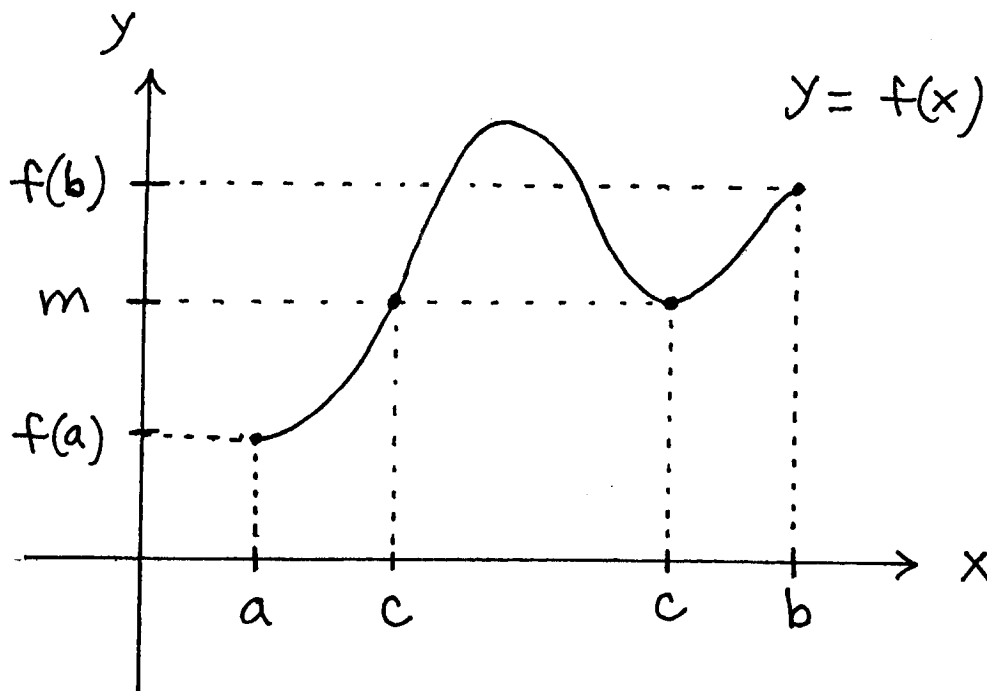


Intermediate Value Theorem (IMVT) : Let  $f$  be a continuous function on the closed interval  $[a, b]$ . Let  $m$  be any number between  $f(a)$  and  $f(b)$ . Then there is at least one number  $c$  in  $[a, b]$  which satisfies

$$f(c) = m .$$



When applying the IMVT to a problem, the following five steps must be clearly established:

1. Define a function  $f$ .
2. Define a number  $m$ .
3. Establish that  $f$  is continuous.
4. Choose an interval  $[a, b]$ .
5. Indicate that  $m$  is between  $f(a)$  and  $f(b)$ .

Once these five steps have been established, the conclusion of the IMVT can be invoked.

## Table for Bisection Method

Let  $f(x) = x^3 + x - 4$ . Goal: Find  $f(x) = 0$  for  $x$  in  $[1, 2]$  up to 2 decimal places.

a	b	$1/2(a+b)$	f(a)	f(b)	$f(1/2(a+b))$
1	2	1.500	-2.000	6.000	0.875
1	1.5	1.250	-2.000	0.875	-0.797
1.25	1.5	1.375	-0.797	0.875	-0.025
1.375	1.5	1.438	-0.025	0.875	0.408
1.375	1.438	1.407	-0.025	0.412	0.189
1.375	1.407	1.391	-0.025	0.192	0.082
1.375	1.391	1.383	-0.025	0.082	0.028
1.375	1.383	1.379	-0.025	0.028	0.001
1.375	1.379	1.377	-0.025	0.001	-0.012

Note: The shaded region represents the choice of new interval in the bisection method.

Conclude:  $x \approx 1.37$  is such that  $f(x) = 0$ .