

Gravity Problems

Defn Let $s(t)$ measure distance at time t

1) $s'(t)$ is instantaneous velocity at time t , usually denoted $v(t) = s'(t)$ with units $\frac{\text{distance}}{\text{time}}$

2) $s''(t)$ is instantaneous acceleration at time t , usually denoted $a(t) = s''(t)$ with units $\frac{\text{distance}}{\text{time}^2}$

For free-falling and projectiles on earth, assuming acceleration is only due to gravity ($g = -32 \text{ ft/sec}^2$), we have the following formulas:

1) $a(t) = s''(t) = -32 \text{ ft/sec}^2$

2) $v(t) = s'(t) = -32t + v_0 \leftarrow \text{initial velocity (i.e. } v_0 = v(0))$

3) $s(t) = -16t^2 + v_0 t + s_0 \leftarrow \text{initial position (i.e. } s_0 = s(0))$

Ex A ball is projected upward at 96 ft/sec from the top of a 256 ft high building.

1) How high does the ball go?

2) How long is ball in the air?

3) What is ball's velocity when:

a) $t = 1 \text{ sec}$ b) it strikes ground