1.) Evaluate $\int_0^2 \int_{(1/2)y}^1 e^{x^2} dx dy$.

2.) Use a triple integral to find the volume of the region D enclosed by the cylinder $(x-1)^2+y^2 = 1$, the plane z = 0, and the plane z = 2 + y.

3.) Let loop C be the triangle with vertices (0,0), (2,0), and (2,6). Evaluate the line integral $\oint xy \, dx + (x-y) \, dy$ two ways :

- a.) directly as a line integral.
- b.) using one of Green's Theorems.

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4.) Let loop C be the circle $x^2 + y^2 = 4$. Use one of Green's Theorems to find the Flux of $\vec{F}(x,y) = (5x)\vec{i} + (-3y)\vec{j}$ across C.

5.) Let surface S be that portion of the cylinder $x^2 + y^2 = 4$ cut by the planes z = 0 and z = 2 + y.

a.) Sketch surface S and parametrize it.

b.) Use a surface integral to find the area of S.

6.) Evaluate the surface integral $\int \int_{S} (xz) \, dS$, where S is given parametrically by $\vec{r}(\phi, \theta) = (\sin \phi \cos \theta) \, \vec{i} + (\sin \phi \sin \theta) \, \vec{j} + (\cos \phi) \, \vec{k}$ for $0 \le \phi \le \pi/4$ and $0 \le \theta \le \pi/2$.

7.) Verify the Divergence Theorem for $\vec{F}(x, y, z) = (y) \vec{i} + (-x) \vec{j} + (-xz) \vec{k}$, where the solid D is enclosed by the paraboloid $z = x^2 + y^2$ and the plane z = 1.

8.) Verify Stoke's Theorem for $\vec{F}(x, y, z) = (x) \vec{i} + (y) \vec{j} + (xz) \vec{k}$, where the surface S is that portion of the plane 2x + 2y + z = 2 lying in the first octant, and the unit normal vector \vec{n} is pointing upward.

The following EXTRA CREDIT PROBLEM is worth . This problem is OPTIONAL.

1.) Assume that curve C is given parametrically by $\vec{r}(t) = (f(t)) \vec{i} + (g(t)) \vec{j} + (h(t)) \vec{k}$ for $t \ge 0$. Let s = s(t) be the arc length of curve C from t = 0 to t. Assume that the unit tangent vector is given by

$$\vec{T}(t) = \vec{T}(t(s)) = (s) \vec{i} + (s^2) \vec{j} + (s^3) \vec{k}$$
.

Find the curvature of C when the arc length is s = 1.