MAT 150A, Fall 2023 Homework 2

Due before 2:10 on Wednesday, October 11

Please write the homework solutions in connected sentences and explain your work. Mark the answers to each question. Scan or take pictures of your homework and upload it to Gradescope before due time.

- **1.** Let x, y, z and w be elements if a group G.
- a) Solve for y given that $xyz^{-1}w = 1$.
- b) Suppose that xyz = 1. Does it follow that yzx = 1? Does it follow that yxz = 1?
- **2.** How many elements of order 2 does the symmetric group S_4 contain?
- **3.** Find the order of the permutation

 $f = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \\ 3 & 10 & 7 & 6 & 2 & 5 & 9 & 4 & 1 & 8 \end{pmatrix}$

4. Determine if the following subset H is a subgroup of G:

a) $G = (\mathbb{Z}, +)$ and H is the set of positive integers.

b) $G = (\mathbb{R}^*, \cdot)$ and H is the set of positive real numbers.

c) G is the set of invertible $n \times n$ matrices and H is the set of $n \times n$ matrices with determinant 1.