

7.

$$\frac{dw}{dt} = \nabla f \cdot \vec{r}'(t)$$

$$\nabla f = \overrightarrow{(2xy, x^2, \cos z)}$$

$$\vec{r}'(t) = \overrightarrow{(2t, 2t, \pi)}$$

$$\vec{r}'(1) = \overrightarrow{(2, 2, \pi)}$$

$$\vec{r}(1) = \overrightarrow{(1, 1, \pi)}$$

$$\text{so } \nabla f(\overrightarrow{(1, 1, \pi)}) = \overrightarrow{(2, 1, \cos \pi)} = \overrightarrow{(2, 1, -1)}$$

$$\nabla f(\overrightarrow{(1, 1, \pi)}) \cdot \overrightarrow{(2, 2, \pi)} = \overrightarrow{(2, 1, -1)} \cdot \overrightarrow{(2, 2, \pi)}$$

$$= 4 + 2 - \pi = 6 - \pi \quad \text{(d)}$$

8.

$$f(x) = \sum_{k=3}^{\infty} 2x^k = 2 \sum_{k=3}^{\infty} x^k = 2 \frac{x^3}{1-x}$$

$$f(-\frac{1}{2}) = 2 \frac{(-\frac{1}{2})^3}{1 - (-\frac{1}{2})} = 2 \frac{-\frac{1}{8}}{\frac{3}{2}} = 2 \cdot \frac{2}{3} \cdot (-\frac{1}{8})$$

$$= -\frac{1}{6} \quad \text{(c)}$$